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TRY NMR WITH YOUR OLD CW RIG

*Using amateur radio equipment to
perform nuclear magnetic resonance
experiments*

Want to try something new and different with your old CW rig? Consider building your own experimental nuclear magnetic resonance (NMR) instrument. With it, you can experience the thrill of sending and receiving radio signals to the protons of hydrogen atoms. As a matter of fact, it's entirely possible to duplicate discoveries made shortly after World War II with that old CW rig of yours, plus a surplus magnet similar to those

that formed part of a radar magnetron. Of course, some readjustment will be necessary to get your old rig tuned to the correct frequency. You'll also need an oscilloscope and an automatic keying circuit.

For those who enjoy construction and troubleshooting, this experiment could be the basis of a science fair project using dated ham rig components. Special interests in RF circuits or computer software are very useful in building

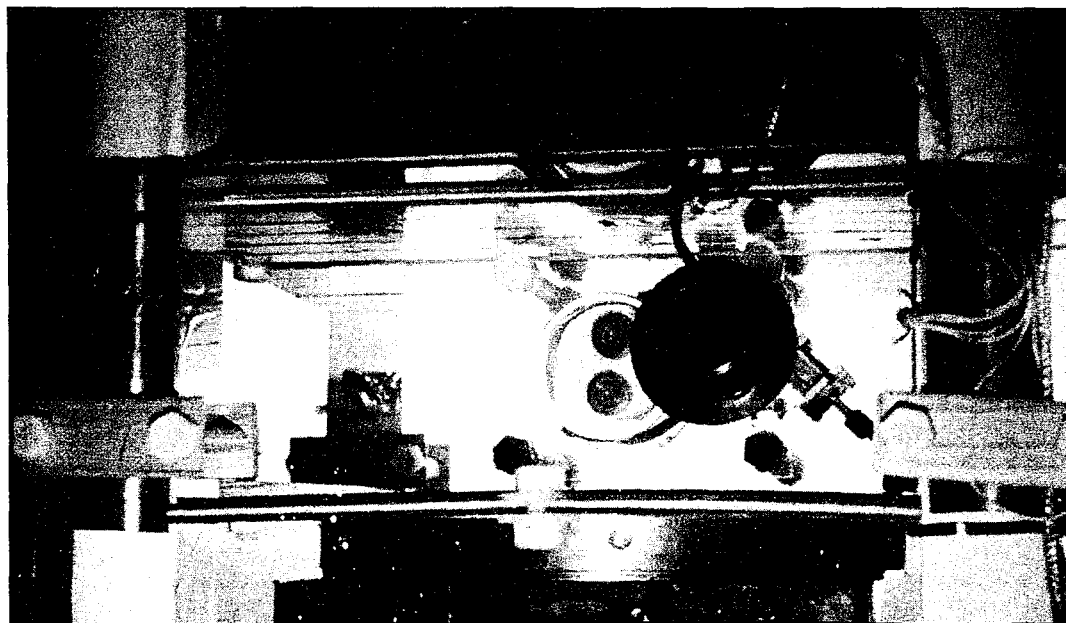


Photo A. Magnet with RF tank coil with two tubes of salad oil. Four steel support columns also serve as the return magnetic field circuit. The field is about 731 Gauss.

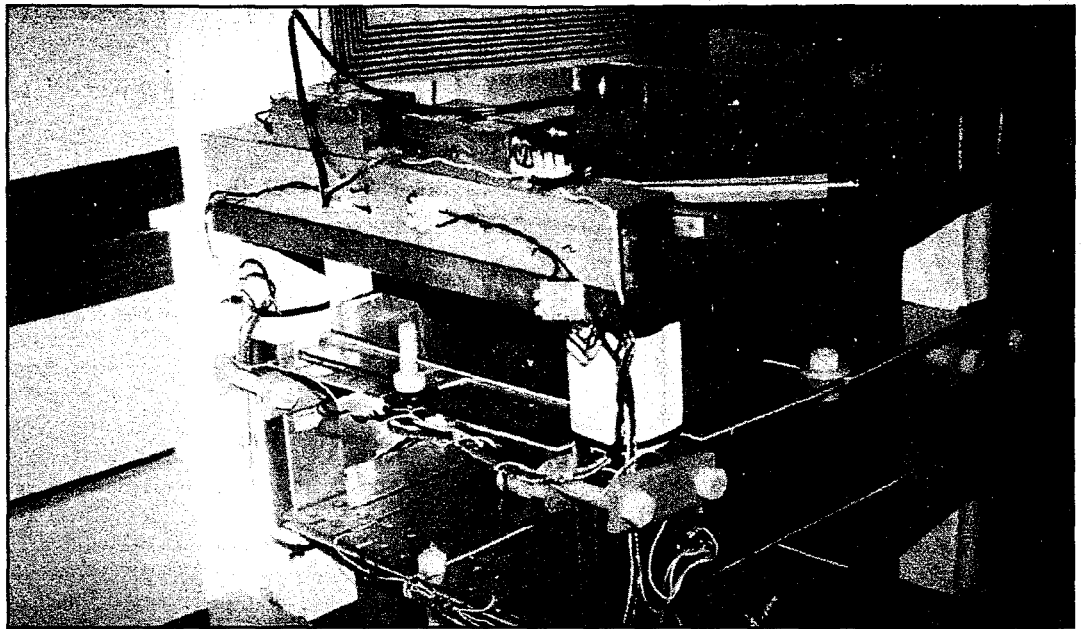


Photo B. The four-poster magnet is 18 inches on each side. A bottle of salad oil is inserted inside a 3.11 tank circuit. Credit cards can be erased if one is not careful.

your own amateur NMR system. **Figure 1** shows a functional block diagram of the major components required to perform amateur NMR.

What is nuclear magnetic resonance?

The hydrogen atom contains one proton at its center. Nuclear magnetic resonance (NMR) and magnetic resonance imaging (MRI) techniques make use of two magnetic fields—a fixed field and a variable radio frequency (RF) field—in a manner that lets an observer make physical measurements based on the proton's reaction to these fields. This method allows one to study the properties of many common substances using components familiar to radio amateurs.

While information on NMR is mostly accessible to those with training in one of the physical sciences, **Reference 1** offers detailed explanations of the fundamentals of NMR using a descriptive, mostly nonmathematical approach. The rapid development of medical MRI systems required that a trained support force be available. This book is often used by institutions to teach support personnel, and is one of several books written to fill this need.

Many atomic nuclei have "spin" and charge. Spin is the atomic equivalent of angular momentum in everyday life. According to quantum theory, a nucleus with spin can only take certain energy levels in a magnetic field. We can visualize the nucleus spinning like a bar magnetic on its axis, producing an associated magnetic field. It is the interaction of this field with external

fields that separates nuclear energy levels and allows NMR to occur. The magnetic moment (current times enclosed area) is sometimes called a nuclear magneton. The hydrogen atom has a 2.79 nuclear magneton value.

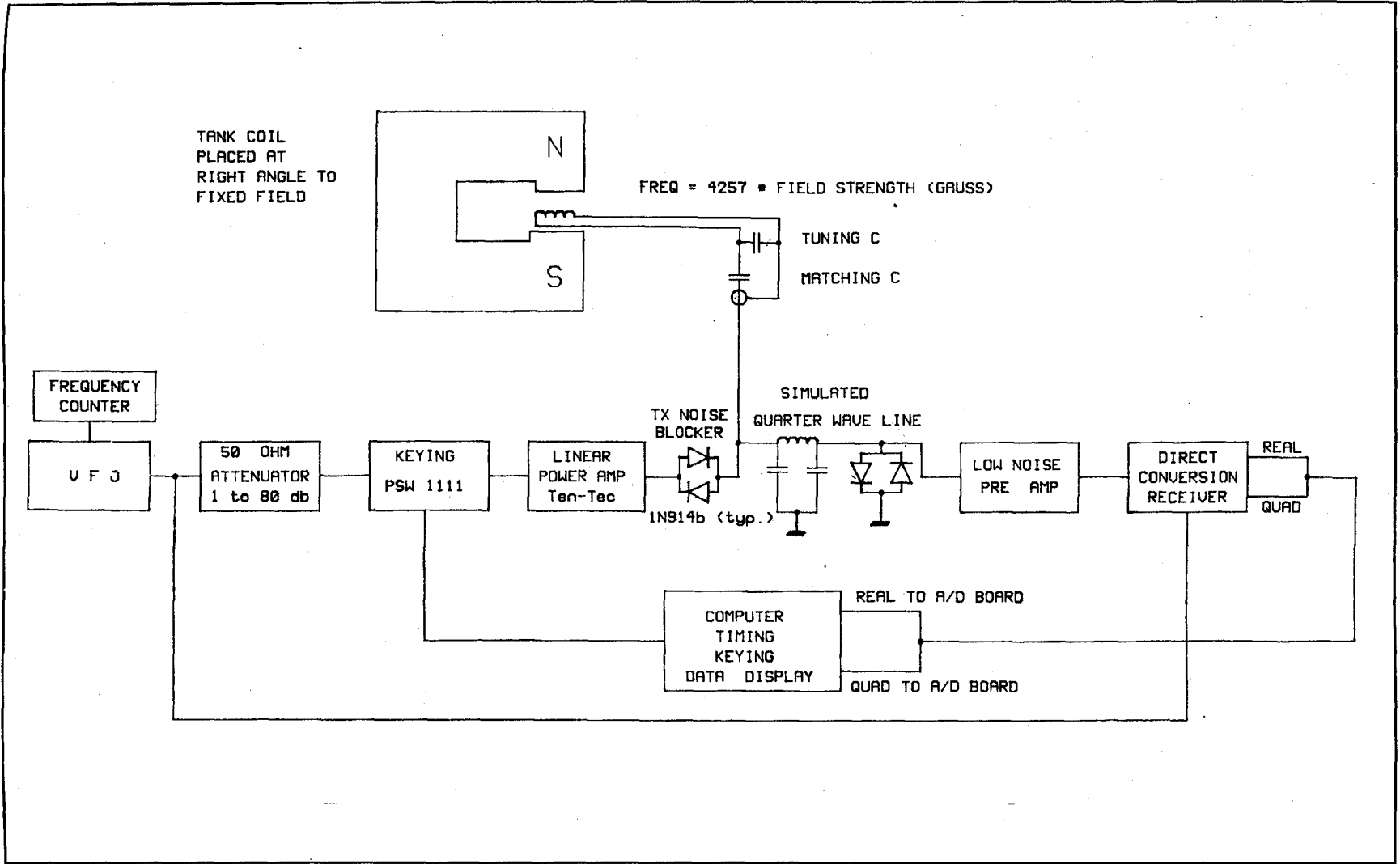
A small bottle of salad oil contains a large number of possible radio signal sources (about 6×10^{22} per cubic milliliter). **Photo A** shows two tubes of salad oil inside a tank circuit between the poles of my magnet. In my magnetic field, only about one atom per million atoms is a potential contributor, on a chance basis, to a detectable RF signal following an RF pulse. A huge number of such atoms results in a detectable signal. The strength of the detected signal can be as much as 5 μ V.

The duration of the RF keying pulse and its power level must be determined by experimentation to find the correct amount of energy to "flip" protons. Best results are obtained when the flip is 90 degrees from the static field. For instance, it's possible to have too great a pulse duration or power level, which might result in flipping the protons 450 degrees, a complete circle plus 90 degrees. The detectable signal would be similar to the correct amount!

Finding a magnet

Magnets are still available from surplus catalogs. When choosing a magnet, remember that the RF signal frequency's purity is a function of the field's uniformity. The magnet's uniformity is equal in importance to its field strength in procuring good results. Obtaining a uniform field is a never-ending goal for NMR and MRI

Figure 1. Functional block amateur NMR system.



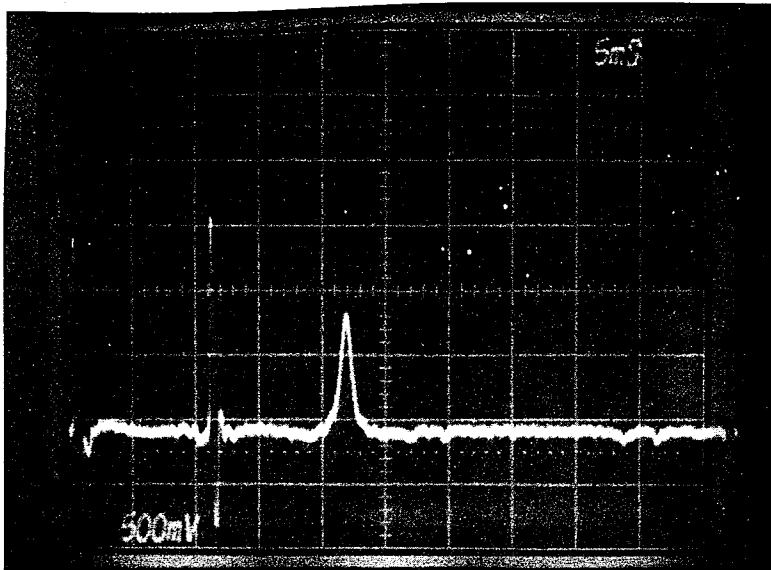


Photo C. A dot/dash RF pulse to the tank coil holding an oil sample in a magnetic field sends back an RF Hahn echo. This is one of the first subjects a new NMR student finds out about (see references).

workers. A tolerance of 5 to 10 parts per million over a volume the size of a golf ball would make a very useful amateur magnet. A change of 1 gauss will mean a change of 4257 Hz in the observed frequency. Moving a metal chair near the magnet can distort the magnetic field and detune your system.

It's even possible to make tests using the Earth's magnetic field at a frequency about 2000 Hz, using audio in place of RF equipment. Perform these tests in your backyard, away from cars or other large metal objects. Several papers appeared during the 1950s

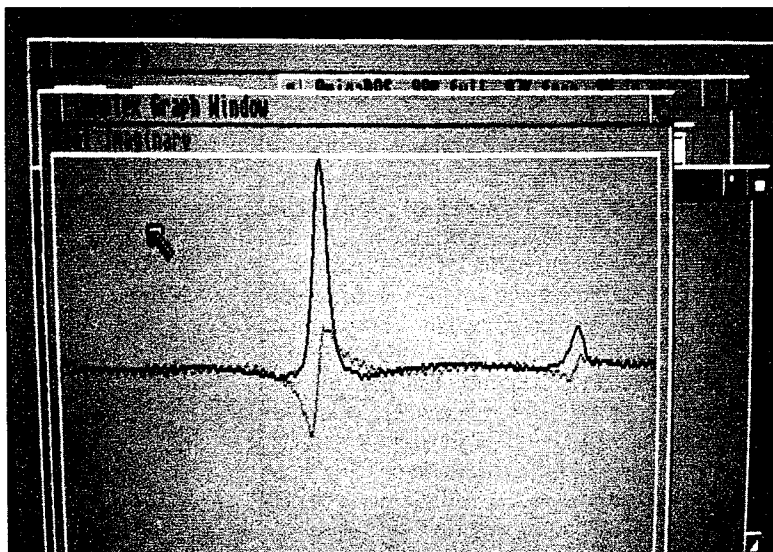


Photo D. Amiga screen shows the real and quadrature of the Hahn echo held RAM memory, this display is the average of 16 echoes. A dual A/D converter board suitable for stereo music will do this nicely.

showing excellent results in measuring small variations in the Earth's magnetic field.²

Simple NMR experiments

The vertical field strength of my 500 pound magnet (see **Photo B**) is about 731 gauss, approximately 1400 times the Earth's magnetic field at my QTH. This magnet is quite temperature sensitive, almost 1 gauss/degree C. I usually have to readjust my master oscillator to find the hydrogen proton frequency if the room temperature changes. My magnet's field strength increases in cold weather.

Once I find the resonant proton frequency, I measure it within one cycle using a frequency counter. This frequency allows a very accurate method of determining the magnetic field strength. The relationship of frequency to magnetic field strength is given by Larmor's constant:

$$f = \text{magnetic field in gauss} \times 4257$$

In my magnet, the NMR frequency is 3.11 MHz, for a field strength of 0.0731T, (The SI unit of Tesla, T, equals 10,000 gauss.) This is near the amateur 80-meter CW band.

My RF tank circuit looks like an 80-meter final tank coil (see **Photo B**). It's driven by short duration RF pulses at 3.11 MHz. When the RF field is applied, the protons spinning in the plane of the static field rotate out of the plane of the field. When the RF field is turned off, the protons return to the plane of the static field, with two degrees of rotational freedom.

The protons' spins, after the RF pulse is turned off, go through a spiral trajectory—like an orange being peeled from one end to the other—emitting a weak RF signal into the resonant tuned tank circuit. The detected RF signal takes the form of a damped sine wave. This damped wave is called a free induction decay (FID), which can last several seconds in a very uniform field, or perhaps only a few milliseconds in a non-uniform field. I sometimes judge the best spot in my magnet by positioning my sample for the longest FID.

This recovery is described by two time constants, T1 and T2, which can be measured later if the data is stored in computer memory. These two time constants, longitudinal (T1) and transverse (T2), describe these return spins to the static field, and can indicate the effect of nearby atomic neighbors on the observed hydrogen protons. For instance in pure water, the two time constants are equal to each other, but this isn't so in salad oil or other complex compounds.

System requirements

The amateur radio requirements needed to

bounce an RF signal off the earth-moon-earth (EME) are equivalent to those required for listening to the proton's spin (see **Figure 1**). As you know, these are a transmitter, receiver, antenna, keyer, a low-noise receiver front end, a T/R system, and a display. The keyer in my system is a computer interface board and software. I use a direct conversion receiver.

I use a computer with a timer board to generate a dot and dash pattern to key the transmitter with the two required pulses—a 90-degree dot followed by a 180-degree dash. The dot lasts 100 μ S and the dash 200 μ S in a typical pattern, with a 25 mS spacing. This is repeated after a 500-mS delay. Several different timing patterns are required to determine the proton spin time constants (T1 and T2). You could try it with a hand key, but you wouldn't get the accuracy you need.

The Hahn echo,³ in **Photos C** and **D**, appearing at 25 mS from my "dot" 90-degree pulse, is captured with a computer analog-to-digital board and stored in computer memory, much as one digitizes a note of music. Later, I use computer software to determine the frequency spectrum (**Photo E**) of the stored echo by Fast Fourier Transform (FFT). The spectrum line width helps me determine the magnetic field uniformity at the position of my sample.

History

I.I. Rabi was known to have been a radio amateur, and was photographed at the controls of this "wireless telegraph" station as a teenager, around 1912.⁴ He's given credit for the general concepts of using two magnetic fields to overcome the field created by the atom's rotating electron, which shields the atomic nucleus. He was awarded an unshared Nobel prize in 1944 for this work, while doing radar development for the war effort. More Nobel awards were presented to others for carrying out advances on this method in the months following the end of World War II using circuits developed by the wartime radar laboratories.⁵⁻⁷ No complete study has been published covering the scientific history of the development of NMR and MRI.

Work in progress

At present, I'm measuring time constants and doing spectrum analysis of Hahn echoes to measure field purity. This should be easy for amateurs to repeat using almost any computer. I did my first Fast Fourier Transform on an Apple II+ based on an article in *BYTE* for viewing music spectrum. This required writing a 6502 machine language FFT routine. This

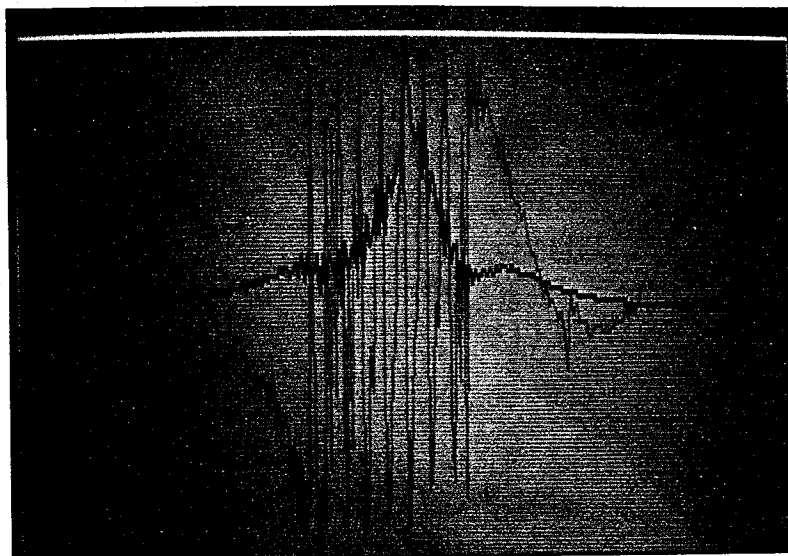


Photo E. Frequency spectrum of Hahn echo shown in **Photo D**, found by using computer software. Baseline is 10 kHz wide. Width at the 50 percent amplitude point is about 200 Hz and may be used to judge magnetic field uniformity. Phase spectrum is shown in background.

allowed the Apple to become my first audio spectrum display about 10 years ago. I hope to obtain my first 2-dimensional MRI picture, perhaps an image of a sectional slice through an orange, soon.

I'll have to develop computer software and gradient amplifiers to drive the gradient coils shown in **Photo A** before this is possible. Complex patterns of gradients and RF pulses are needed to acquire a 2-D image plane, which must then be "decoded" using 2-dimensional spectrum analysis. With the help of Dave Reddy, N1RBJ, I've developed computer software that will perform a double-precision 128 x 128 2-D FFT on a generic 486DX 66-MHz PC clone in about 4 seconds—much faster than the expensive array processors used for these kinds of reconstructions in the recent past.

We've tested this software by reconstructing raw data of a water-bottle phantom originally acquired on a Yale University experimental NMR system. **Photo F** shows the raw data, which looks like ripples spreading in water, and **Photo G** depicts the finished magnitude and phase images. Note that the finished images are inverted, and the air bubble at the top of the bottle with its meniscus is shown at the bottom.

Summary

If you're interested in transmitters, receivers, or computer software, you'll find the effort required to capture the radio signals emitted by the proton's spin a challenge. Everything I've done can be recreated using common amateur

↑
USING
DAVID
REDDY'S
PROGRAMS

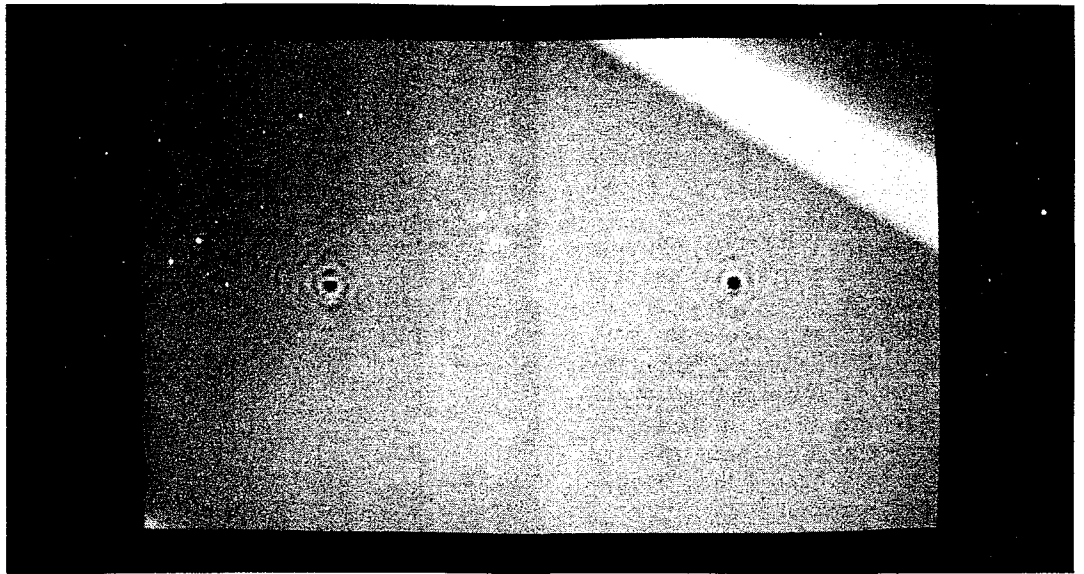


Photo F. Raster display of two 64K arrays showing RF data received from an oil sample. MRI images look like holo-grams before the 2-D FFT data reduction. This represents a 128 x 128 x 12 bit array.

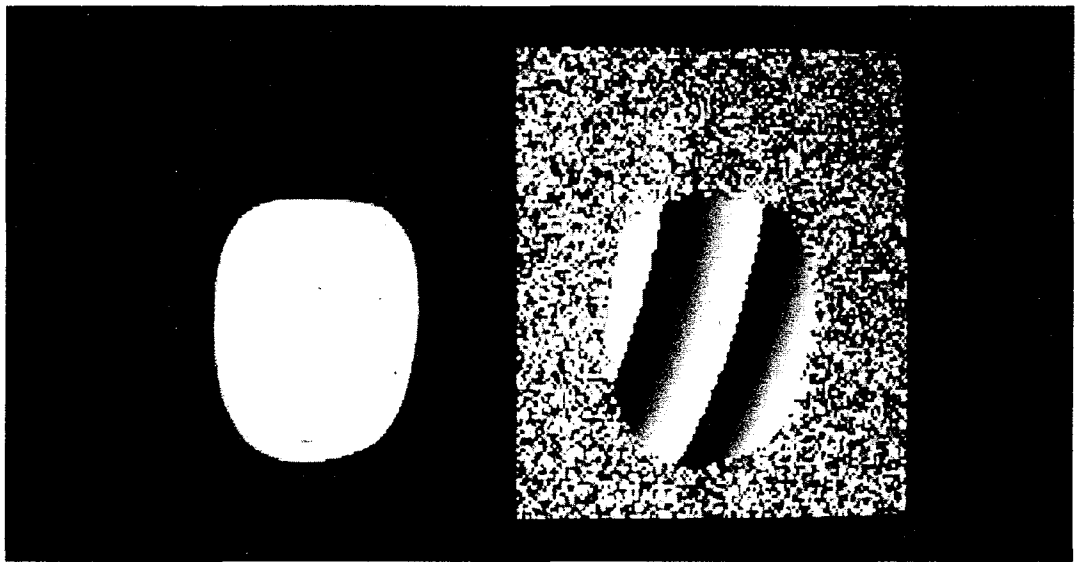


Photo G. After a 2-D FFT computer analysis (*Photo F*) shows a cross-sectional slice through the oil sample bottle. These two images now occupy the same memory space as the images in *Photo F*. Process requires 4 seconds on a 486DX 66-MHz computer.

parts, a magnet, and some patience. Amateurs with RF circuit and computer experience are well-equipped to learn about NMR. I had to learn many new terms—like Larmor's Constant, FFT, FID, T1, T2, and many others—before I was comfortable with this new field that uses RF and computer equipment to perform tasks which would have been material for science fiction stories not too many years ago. ■

REFERENCES

1. H.J. Smith and F.N. Ranallo, *A Non-Mathematical Approach to Basic MRI*, Medical Physics Pub. Corp., 1989.
2. G.S. Waters, "A Measurement of the Earth's Magnetic Field by Nuclear Induction," *Nature*, 73:691, 1955.
3. E.L. Hahn, *Physics Review* 270: 80, 1950.
4. J.S. Rigden, *Rabi Scientist and Citizen*, Basic Books, Inc., 1989.
5. C.L. Stong, "How amateurs can build a simple magnetic resonance spectrometer," *Scientific American* 200:171-178, April 1959.
6. G.E. Pake, "Magnetic Resonance," *Scientific American*, pages 58-66, August 1958.
7. I.L. Pykett, "NMR Imaging in Medicine," *Scientific American* 246:78-88, May 1982.

Fast Fourier for the 6800

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If you're involved with music or speech processing applications with your computer, you've probably wished you could look at the frequency spectrum of your sampled signals. This may not be as difficult as you might guess, because here is a simple, straightforward fast Fourier transform (FFT) subroutine that can do the trick in just a few seconds.

A Microhistory of the Fast Fourier Transform

The analysis of waveforms for harmonic content has a long and fascinating history. Bernoulli and Euler developed the mathematics of the transform while experimenting with musical strings in 1728, nearly a hundred years before Jean Baptiste Fourier gave his name to the equations. Interest in prediction of the tides led Lord Kelvin to build a mechanical harmonic synthesizer that inspired the construction of increasingly complex mechanical harmonic analyzing machines. This trend culminated in the Mader-Ott machine of 1931, which is on display at the Smithsonian Institute in Washington DC.

With the growth of the telephone and the communication industry came sampling theory and the *discrete Fourier transform*. At first, discrete Fourier transforms were hand calculated and tabular forms called "schedules" were soon employed to speed the process. With the development of digital computers in the 1940s this task became somewhat easier to perform. The number of calculations required still made the concept of real time discrete Fourier transforms unlikely even on the ever faster new computers.

Then in the 1960s a number of matrix theory mathematicians, including J W Cooley and J W Tukey, went back to the "schedules" and discovered that a great many of the terms were redundant and could be factored out. The procedure they evolved became known as the *fast Fourier transform*, which reduces the number of calculations to the point that special hardware can be built to perform the transform in real time and display the frequency spectrum continuously on a video display.

The Basic Concepts

A number of books have been published describing the mathematics of the fast Fourier transform in some detail. A few of these contain sample programs in FORTRAN, ALGOL, or BASIC. However, the use of a high level language to perform this computation not only costs a great deal in speed and efficiency, but also obscures the simple binary processes that characterize the algorithm. Since high level languages do not usually support bit manipulation, these processes can become almost as time consuming as the arithmetic.

Clearly, assembly language programming of the fast Fourier transform offers many advantages, but the literature seldom provides any examples of assembly level code to illustrate how the equations are implemented. Thus the program described in this article may well be the reinvention of someone else's "wheel"

The details of the inner workings of the fast Fourier transforms are left to the technical references, but the basic concepts are not difficult to grasp. The transform involves complex products which behave in the manner of the coordinates of a rotating vector. When this vector is at angles which are multiples of 90 degrees, the sine and cosine terms of the equations become +1, 0, or -1. Since terms containing these values do not require computed multiplication, the arithmetic becomes very simple. Other terms cancel each other out in order to simplify the equations at other angles. By factoring these terms out of the transform, many unnecessary calculations may be eliminated.

The input data may be thought of as elements of an input matrix which will be multiplied by a transform matrix. The product is a matrix containing the transformed data. The redundant elements may be factored out of the transform matrix, converting it to the product of a number of simpler transforms. For an input array of 256 points, a discrete Fourier transform would require 256 by 256 complex products or 262,144 binary multiplications. The fast Fourier transform reduces this to eight simpler trans-

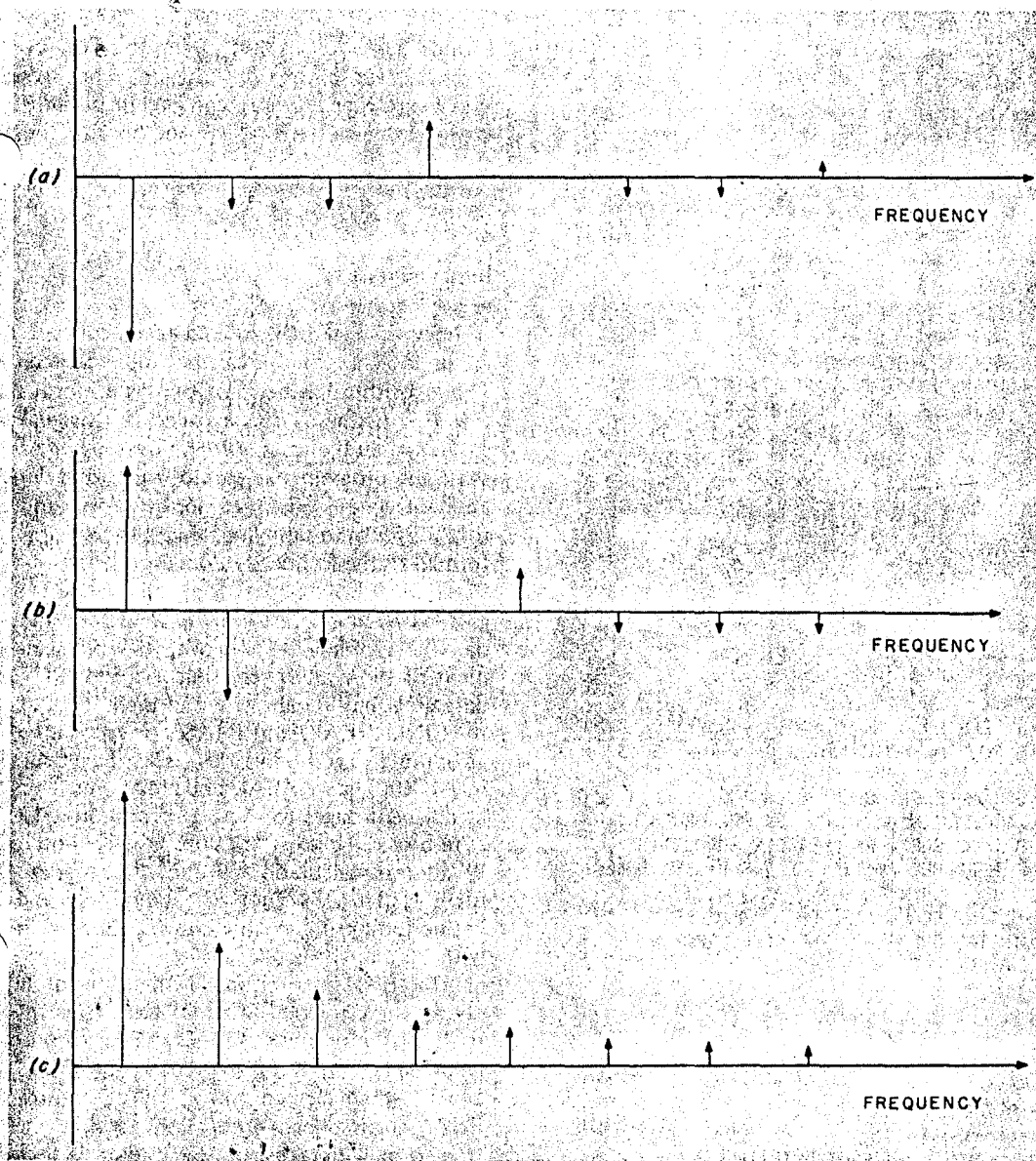


Figure 1: Fast Fourier transform of a square wave using the author's technique. The real (or sine) part of the transform is shown in (a). The imaginary (or cosine) part of the transform is shown in (b). The resulting transform is at (c). The resulting transform values are normally found by taking the square root of the sum of the squares of the cosine and sine elements. In order to save computational time, however, the author takes the sum of the absolute values of the terms, which introduces slight errors into the relative magnitudes of the components.

forms and ultimately requires 8 by 2 by 256 complex products, or 16,384 binary multiplications (1/16 the number of previous multiplications). Even greater savings are realized as the number of points increases.

Each of the simplified transforms operates on the data in pairs of complex points. The real and imaginary parts of a pair are transformed and the new values placed back in the array so that the transform is performed "in place." The algorithm then moves on to the next pair until all pairs have been transformed. The process is repeated for each of the eight stages of our 256 point transform, but on each pass the distance between pairs is changed.

On the first pass, adjacent points are paired. After completing a pair the algorithm skips down to the next. In a sense, the data has been split into 128 adjacent 2 point transforms. These 128 groups are known as

cells. On each subsequent pass the distance between elements of the pair is doubled. In the second pass there are 64 cells, each four elements wide. On the final pass there is only one cell containing all 256 elements.

This process of forming pairs and cells causes the elements of the array to become scrambled. On the final pass the data is completely mixed up and must be sorted out before it can be used. The way it is scrambled is very interesting, though. If each element is assigned a binary number that represents its location in the array, the scrambled data makes it appear that the computer has read this binary address backwards. It is as if the binary word were swapped end for end so the most significant bit (MSB) appears where the least significant bit (LSB) should be.

This rearrangement of the data may be corrected by swapping each data point with its bit reverse addressed mate. The procedure

Listing 1: Routine in 6800 assembly language to perform a 256 point fast Fourier transform.

```

00001          NAM      FFT#2
00002          OPT      O, S, NOGEN
00003          *****
00004          ** FAST FOURIER **
00005          ** TRANSFORM **
00006          ** SUBROUTINE **
00007          *****
00008          ** BY R. H. LORD **
00009          ** 21 APRIL, 1978 **
00010          *****
00011          **
00012          ** THIS SUBROUTINE PERFORMS A 256 POINT FFT
00013          ** ON THE DATA IN THE INPUT DATA TABLE.
00014          ** INPUT DATA IS ASSUMED TO BE TWO'S COMPLEMENT.
00015          ** THE SUBROUTINE GENERATES A COSINE (REAL) AND SINE
00016          ** (IMAGINARY) DATA TABLE AT "REAL" AND "IMAG"
00017          ** THE RESULTANT TRANSFORM DATA IS 128 POINTS
00018          ** SYMMETRICALLY REFLECTED ABOUT THE CENTER OF
00019          ** THE 256 POINT TABLE.
00020          **
00021          ** THE SUBROUTINE ASSUMES THAT THE INPUT DATA
00022          ** IS ALL REAL AND THEREFORE DOES NOT MANIPULATE
00023          ** THE IMAGINARY PORTION UNTIL AFTER THE FIRST
00024          ** PASS.
00025          **
00026          ** ALL DATA AREAS MUST BE ON PAGE BOUNDARIES (XX00)
00027          ** SINCE THE ROUTINE MANIPULATES ONLY THE LSB'S.
00028          **
00029          ** THE TWO'S COMPLEMENT MULTIPLICATION IS KEPT AS A
00030          ** SEPARATE SUBROUTINE. IT MAY BE PERFORMED WITH
00031          ** A CONVENTIONAL SOFTWARE MULTIPLY SUBROUTINE
00032          ** OR WITH A HARDWARE MULTIPLIER FOR HIGHER SPEED.
00033          **
00034          ** THE SUBROUTINE SCALES THE DATA WHENEVER
00035          ** IT ANTICIPATES OVERFLOW. THE SCALE FACTOR
00036          ** COUNT IS AVAILABLE IN "SCLFCT".
00037          **
00038          **
00039          **
00040          **
00041          *****
00042          ** DATA AREAS **
00043          *****
00044          0000 EQU $0000 INPUT DATA TABLE
00045          0500 REALT EQU $0500 "REAL" DATA TABLE
00046          0600 IMAGT EQU $0600 "IMAG" DATA TABLE
00047          0400 SINET EQU $0400 SINE LOOKUP TABLE
00048          *****
00050          0020 ORG $0020
00051          *****
00052          ** BASE PAGE PTRS **
00053          *****
00054          0020 0002 RLPT1 RMB 2 "REAL" DATA POINTERS
00055          0022 0002 RLPT2 RMB 2
00056          0024 0002 IMPT1 RMB 2 "IMAG." DATA POINTERS
00057          0026 0002 IMPT2 RMB 2
00058          0028 0002 SINPT RMB 2 SINE TABLE POINTER
00059          002A 0001 CELNUM RMB 1 CELLS FOR THIS PASS
00060          002B 0001 CELCT RMB 1 CELL COUNTER FOR PASS
00061          002C 0001 PAIRNM RMB 1 PAIRS/CELL
00062          002D 0001 CELDIS RMB 1 CELL OFFSET(DISTANCE)
00063          002E 0001 DELTA RMB 1 ANGLE INCREMENT
00064          002F 0001 SCLFCT RMB 1 SCALE FACTOR CTR.
00065          0030 0001 COSA RMB 1 TEMPORARY COSINE
00066          0031 0001 SINA RMB 1 TEMPORARY SINE
00067          0032 0001 TREAL RMB 1 TEMP. REAL DATA
00068          0033 0001 TIMAG RMB 1 TEMP. IMAG DATA
00069          0034 0001 MSBY RMB 1 MULTIPLY MSB
00070          0035 0001 LSBY RMB 1 MULTIPLY LSB
00071          0036 0004 MPA RMB 4 SOFTWARE MPY ACCUM.
00072          *****

```

is called "bit swapping" and may be performed either at the end of the fast Fourier transform or before it is begun. The pre-transform swap is more convenient because less points need be swapped and because the vector rotation within each cell is simpler. In the posttransform version the vector angles would also have to be bit swapped.

Implementation

Now that we have looked at the concept, let us look at how it can be implemented. The algorithm has been written as a subroutine (see listing 1) to be called by a signal gathering and display program. It assumes that this program has stored some time dependent data in 2's complement form and that a 256 byte sample of this is to be transformed to the frequency domain.

The fast Fourier transform subroutine begins with an address lookup table for the data areas. This table makes the reassignment of these areas very simple. The INPUT data area may be anywhere in memory, but the SINE, REAL, and IMAG arrays must be at address page boundaries (ie: at hexadecimal XX00), and REAL and IMAG must be in adjacent pages forming a continuous 512 byte block. These restrictions greatly simplify address calculation within the program. SINE is the address of a 256 byte sine and cosine lookup table which must be loaded in with the transform subroutine.

The first instruction of the subroutine clears the variable SCLFCT which keeps track of the number of times the data has to be scaled to prevent overflow. The IMAG array is then cleared and at MOVE the INPUT data is copied into REAL, where the transform will take place. The data is then prescrambled to put it in bit reverse order for the transform process. The bit reversed address is calculated by rotating the least significant bit of the address into the carry and rotating the reversed address out in the opposite direction. The new address is compared with the first address to prevent swapping the data back to the original order, then the two array elements are exchanged.

Once the swapping is complete, the data is ready to be transformed. The fast Fourier transform is performed in eight separate passes; before each pass begins, the data is tested by SCALE to prevent any overflow. For the first pass there are 128 cells formed by adjacent pairs of data. In this pass the vector angle steps in multiples of 180 degrees. This means that all the sine terms are 0 and the cosine terms are either +1 or -1. Also there is no data yet in the IMAG array. The general equations thus become greatly simplified and the pass is reduced to addition and subtraction among elements of the

Listing 1, continued:

```

00073      ** START OF TRANSFORM      **
00074      *****
00075 0200      ORG      $0200
00076 0200 20 08      BRA      START      JUMP AROUND PARAMETERS
00077      *****
00078      ** ADDRESS LOOK-UP TABLE **
00079      ** FOR DATA AREAS      **
00080      *****
00081 0202 0800      INPD   FDB      INPUT   SET UP DATA AREAS
00082 0204 0500      REAL   FDB      REALT
00083 0206 0600      IMAG   FDB      IMAGT
00084 0208 0400      SINE   FDB      SINET
00085      *****
00086      **
00087 020A 7F 002F      START  CLR      SCLFCT  NOTHING SCALED YET
00088      **
00089      *****
00090      ** INPUT DATA SET-UP      **
00091      *****
00092 0200 FE 0206      CLEAR  LDX      IMAG      CLEAR OUT IMAG.
00093 0210 5F          CLR      CLR B      SET UP COUNTER
00094 0211 6F 00      CLR1   CLR      0,X      CLEAR MEMORY
00095 0213 08          INX
00096 0214 5A          DEC B
00097 0215 26 FA          BNE      CLR1
00098 0217 FE 0202      MOVE   LDX      INPD      SET UP POINTERS
00099 021A DF 20          STX     RLPT1
00100 021C FE 0204          LDX     REAL
00101 021F DF 22          STX     RLPT2
00102 0221 DE 20          MOV1   LDX      RLPT1     MOVE INPUT DATA
00103 0223 A6 00          LDA A   0,X      TO "REAL" ARRAY
00104 0225 08          INX
00105 0226 DF 20          STX     RLPT1
00106 0228 DE 22          LDX     RLPT2
00107 022A A7 00          STA A   0,X
00108 022C 7C 0023          INC     RLPT2+1
00109 022F 26 F0          BNE     MOV1     TEST PAGE OVERFLOW
00110      *****
00111      ** PRE-TRANSFORM BIT SWAP **
00112      *****
00113 0231 FE 0204          LDX     REAL      SET UP DATA POINTERS
00114 0234 DF 20          STX     RLPT1
00115 0236 DF 22          STX     RLPT2
00116 0238 C8 08          BITREV LDA B   #8      SET BIT COUNTER
00117 023A 96 21          LDA A   RLPT1+1     GET POINTER 1
00118 023C 46          BRV1   ROR A      REVERSE BIT ORDER
00119 023D 79 0023          ROL     RLPT2+1     FOR SECOND POINTER
00120 0240 5A          DEC B      COUNT BITS
00121 0241 26 F9          BNE     BRV1
00122 0243 96 23          LDA A   RLPT2+1     GET REVERSED BYTE
00123 0245 91 21          CMP A   RLPT1+1     COMPARE WITH #1
00124 0247 25 0E          BCS     SWP1       BRANCH IF ALREADY SWAPPED
00125 0249 DE 20          SWAP   LDX     RLPT1     GET POINTER 1
00126 024B A6 00          LDA A   0,X      GET VAL 1
00127 024D DE 22          LDX     RLPT2     GET POINTER 2
00128 024F E6 00          LDA B   0,X      GET VAL 2
00129 0251 A7 00          STA A   0,X      REPLACE WITH VAL 1
00130 0253 DE 20          LDX     RLPT1     GET FIRST POINTER
00131 0255 E7 00          STA B   0,X      COMPLETE SWAP
00132 0257 7C 0021      SWP1   INC     RLPT1+1     DO NEXT POINT PAIR
00133 025A 26 DC          BNE     BITREV     UNLESS ALL ARE DONE
00134      *****
00135      ** FFT FIRST PASS      **
00136      *****
00137      ** SINCE IN PASS 1 ALL ANGLES      **
00138      ** ARE MULTIPLES OF 180 DEG.      **
00139      ** THERE ARE NO PRODUCT TERMS.      **
00140      ** AND NO IMAGINARY TERMS YET      **
00141      ** HENCE A FAST VERSION OF PASS 1 **
00142      *****
00143 025C BD 0333      PASS1 JSR     SCALE     SCALE IF ANY OVER-RANGE DATA

```

REAL array. Considerable time is saved by making this pass separate and bypassing the unneeded table lookup and multiply routines.

Once this pass is completed, the arithmetic gets much more complex. The remaining seven passes are performed by a general fast Fourier transform algorithm. It begins at FPASS by setting up 64 cells of four elements with the pairs separated by two units. The vector angle is set to increment by 90 degrees by setting DELTA to 64. At NPASS, the pointers are set up for the first cell and the pass then begins with a sine and cosine table lookup. The complex data pair is then processed using the standard fast Fourier transform equations:

$$TR = RN \cos(w) + IN \sin(w)$$

$$TI = IN \cos(w) - RN \sin(w)$$

$$RM' = RM + TR \quad RN' = RM - TR$$

$$IM' = IM + TI \quad IN' = IM - TI$$

After each pair has been transformed the angle is incremented by DELTA and the next pair processed. When all pairs in a cell have been transformed the routine moves down to the next cell and returns to NCELL to continue the process. When the last cell has been done, CELCT becomes 0 and the pass is complete.

At the end of each pass the number of cells and the angle increment are divided in half and the pair separation and number of pairs per cell are doubled. The whole process is then repeated by branching to NPASS until the end of the last pass when the number of cells becomes 0. The routine then branches to DONE and returns to the calling program.

The SCALE subroutine is used to anticipate and prevent overflow of the 8 bit data. It is called before each pass and begins by testing the value of each data point. If any point exceeds the range of -64 to +64 the subroutine branches to SCL4 where the entire array is scaled down by a factor of 2. The variable SCLFCT is incremented to indicate the total number of times the data has been scaled.

The multiply routine has been placed at the end of the program to make substitution of other versions easy. The original program was written for a hardware multiplier similar to the device described by Bryant and Swasdee in April 1978 BYTE, page 28. To eliminate the need for such exotic hardware, a software multiply routine has been substituted with some increase in transform time. After the multiplication is completed

Listing 1, continued:

```

00144 025F FE 0204      LDX  REAL    SET UP POINTERS
00145 0262 DF 20        STX  RLPT1
00146 0264 DE 20  PA1  LDX  RLPT1    GET POINTER
00147 0266 A6 00        LDA  A 0,X    GET RM
00148 0268 E6 01        LDA  B 1,X    AND RN
00149 026A 36          PSH  A        SAVE RM
00150 026B 1B          RBA          RM'=RM+RN
00151 026C A7 00        STA  A 0,X    STORE NEW RM'
00152 026E 32          PUL  A        GET OLD RM
00153 026F 10          SBA          RN'=RM-RN
00154 0270 A7 01        STA  A 1,X    STORE RN'
00155 0272 7C 0021     INC  RLPT1+1  MOVE TO NEXT PAIR
00156 0275 7C 0021     INC  RLPT1+1
00157 0278 26 EA      BNE  PA1     KEEP GOING TILL DONE
00158
00159      *****
00160      ** COMPUTATION OF FFT **
00161      ** PASS 2 THRU N **
00162 027A 86 40  FPASS LDA  A #64    SET UP PARAMETERS
00163 027C 97 2A      STA  A CELNUM  FOR CELL COUNT
00164 027E 97 2E      STA  A DELTA   AND ANGLE
00165 0280 86 02      LDA  A #2      AND FOR
00166 0282 97 2C      STA  A PAIRNM  PAIRS/CELL
00167 0284 97 2D      STA  A CELDIS  DISTANCE BETWEEN PAIRS
00168 0286 BD 0333  NPASS JSR  SCALE     KEEP DATA IN RANGE
00169 0289 96 2A      LDA  A CELNUM  GET NUMBER OF CELLS
00170 028B 97 2B      STA  A CELCT   PUT IN COUNTER
00171 028D FE 0204     LDX  REAL     SET UP POINTERS
00172 0290 DF 20      STX  RLPT1
00173 0292 DF 22      STX  RLPT2
00174 0294 FE 0206     LDX  IMAG
00175 0297 DF 24      STX  IMPT1
00176 0299 DF 26      STX  IMPT2
00177 029B FE 0208  NCELL LDX  SINE
00178 029E DF 28      STX  SINPT
00179 02A0 D6 2C      LDA  B PAIRNM  GET PAIRS/CELL CTR
00180 02A2 96 21  NC1  LDA  A RLPT1+1 GET POINTER 1 LSBY
00181 02A4 98 2D      ADD  A CELDIS  ADD PAIR OFFSET
00182 02A6 97 23      STA  A RLPT2+1 SET BOTH POINTER 2'S
00183 02A8 97 27      STA  A IMPT2+1
00184 02AA 37          PSH  B        SAVE PAIR CTR
00185 02AB DE 28      LDX  SINPT    SET UP SINE LOOKUP
00186 02AD A6 00      LDA  A 0,X    GET COSINE OF ANGLE
00187 02AF 97 30      STA  A COSA   SAVE ON BASE PAGE
00188 02B1 A6 40      LDA  A 64,X   GET SINE
00189 02B3 97 31      STA  A SINA   AND SAVE IT
00190 02B5 DE 22      LDX  RLPT2    GET "REAL" POINTER 2
00191 02B7 A6 00      LDA  A 0,X    GET RN
00192 02B9 36          PSH  A        SAVE IT
00193 02BA D6 30      LDA  B COSA   GET COSINE
00194 02BC BD 036A     JSR  MPY      MAKE RN*COS(A)
00195 02BF 97 32      STA  A TREAL  SAVE IT
00196 02C1 32          PUL  A        RESTORE RN
00197 02C2 D6 31      LDA  B SINA   GET SINE
00198 02C4 BD 036A     JSR  MPY      RN*SIN(A)
00199 02C7 97 33      STA  A TIMAG
00200 02C9 DE 26      LDX  IMPT2    GET IMAG. POINTER 2
00201 02CB A6 00      LDA  A 0,X    GET IN
00202 02CD 36          PSH  A        SAVE IT
00203 02CE D6 31      LDA  B SINA   GET SINE
00204 02D0 BD 036A     JSR  MPY      IN*SIN(A)
00205 02D3 9B 32      ADD  A TREAL  TR=RN*COS+IN*SIN
00206 02D5 97 32      STA  A TREAL
00207 02D7 32          PUL  A        RESTORE IN
00208 02D8 D6 30      LDA  B COSA   GET COSINE
00209 02DA BD 036A     JSR  MPY      IN*COS(A)
00210 02DD 90 33      SUB  A TIMAG  TI=IN*COS-RN*SIN
00211 02DF 97 33      STA  A TIMAG
00212 02E1 DE 20      LDX  RLPT1
00213 02E3 A6 00      LDA  A 0,X    GET RM
00214 02E5 16          TAB          SAVE IT

```

the data must be scaled up by a factor of 2. This is because the sine and cosine terms represent fractional binary values. The least significant bit is shifted in from the lower byte to preserve accuracy.

Analyzing the Results

After working with all this mathematics and software, what do you end up with? We started with a 256 point time domain sample in REAL. The fast Fourier transform converts this to a frequency domain sample corresponding to the spectrum of the input. The first element of each array represents the DC component of the input. The next element represents the sine wave with period equal to the duration of the input sample. Each remaining element depicts a multiple of this frequency until the middle of the array is reached, representing 128 cycles per period. The remainder of the array is symmetrical to the first 128 points.

Each element in the REAL and IMAG arrays represents information about one frequency component of the input sample. But why do we end up with two arrays, and what do the cosine terms of REAL and the sine terms of IMAG really mean to us? Usually this information is described in terms of amplitude and phase of the component, and often the phase information is of little interest. The cosine and sine terms represent the X and Y components of a vector with length and angle equal to the amplitude and phase terms that we are after. All we have to do is find the length of the vector from the square root of the sum of squares of the cosine and sine terms.

The only problem is that this calculation requires almost as much time as the transform, due to the square root. If we bypass the root and display the sum of squares (the power spectrum) we miss most of the detail of the lesser components. I have found that the highly unmathematical solution of displaying the sum of the absolute values is fairly satisfactory, although it introduces some error in the relative amplitude of peaks. This value is then sent to a digital to analog converter for display on an oscilloscope.

Putting the Fast Fourier Transform to Work

This program has a number of interesting applications for speech recognition, image processing, and the synthesis of musical instruments. A recent issue of *The Computer Music Journal* even describes a program for transcribing recordings back into sheet music (see bibliography, page 118).

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Listing 1, continued:

00215	02E6	9B	32	ADD A	TREAL	RM'=RM+TR	
00216	02E8	A7	00	STA A	0,X		
00217	02EA	DE	22	LDX	RLPT2		
00218	02EC	D0	32	SUB B	TREAL	RN'=RM-TR	
00219	02EE	E7	00	STA B	0,X		
00220	02F0	DE	24	LDX	IMPT1		
00221	02F2	A6	00	LDA A	0,X	GET IM	
00222	02F4	16		TAB		SAVE IT	
00223	02F5	9B	33	ADD A	TIMAG	IM'=IM+TI	
00224	02F7	A7	00	STA A	0,X		
00225	02F9	DE	26	LDX	IMPT2		
00226	02FB	D0	33	SUB B	TIMAG	IN'=IM-TI	
00227	02FD	E7	00	STA B	0,X		
00228	02FF	96	29	LDA A	SINPT+1	INCREMENT ANGLE	
00229	0301	9B	2E	ADD A	DELTA		
00230	0303	97	29	STA A	SINPT+1		
00231	0305	7C	0021	INC	RLPT1+1	INCREMENT POINTERS	
00232	0308	7C	0025	INC	IMPT1+1		
00233	030B	33		PUL B		GET PAIR COUNTER	
00234	030C	5A		DEC B		DECREMENT	
00235	030D	26	93	BNE	NC1	DO NEXT PAIR	
00236	030F	96	21	LDA A	RLPT1+1	GET POINTERS	
00237	0311	9B	2D	ADD A	CELDIS	ADD CELL OFFSET	
00238	0313	97	21	STA A	RLPT1+1		
00239	0315	97	25	STA A	IMPT1+1		
00240	0317	7A	002B	DEC	CELCT	DECR. CELL COUNTER	
00241	031A	27	03	BEQ	NP1	NEXT PASS?	
00242	031C	7E	029B	JMP	NCELL	NO. DO NEXT CELL	
00243				**			
00244				**	CHANGE PARAMETERS FOR NEXT PASS	**	
00245				**			
00246	031F	74	002A	NP1	LSR	CELNUM	HALF AS MANY CELLS
00247	0322	27	0C	BEQ	DONE		NO MORE CELLS
00248	0324	78	002C	ASL	PAIRNM		TWICE AS MANY PAIRS
00249	0327	78	002D	ASL	CELDIS		TWICE AS FAR APART
00250	032A	74	002E	LSR	DELTA		HALF THE ANGLE
00251	032D	7E	0286	JMP	NPASS		DO NEXT PASS
00252				*****			
00253				**	END OF FFT ROUTINE	**	
00254				*****			
00255				**			
00256	0330	39		DONE	RTS		EXIT FFT SUBROUTINE
00257	0331	0002			RMB	2	ROOM FOR JUMP EXIT
00258				**			
00259				*****			
00260				**	OVER-RANGE DATA SCALE	**	
00261				*****			
00262	0333	FE	0204	SCALE	LDX	REAL	SET UP DATA POINTER
00263	0336	5F			CLR B		SET UP PAIR CTR
00264	0337	37		SCL1	PSH B		SAVE PAIR CTR.
00265	0338	C6	02		LDA B	#2	SET UP PAIR
00266	033A	A6	00	SCL2	LDA A	0,X	GET DATA
00267	033C	08			INX		BUMP POINTER
00268	033D	31	08		CP	#02	TEST LOWER LIMIT
00269	033E	31	08		CP	#02	SKIP TO NEXT POINT
00270	0341	01	08		CP	#5A8	TEST UPPER LIMIT
00271	0343	24	08		BCC	SCL4	SCALE IF OUT OF RANGE
00272	0345	5A			DEC B		TEST NEXT POINT

Listing 1, continued:

To get meaningful information from the transform, the input data must be sampled judiciously. While this program in theory is capable of analyzing 128 harmonics of a given sample, this is only true when the input represents exactly one complete cycle of the waveform being analyzed. Most data just doesn't come packaged that way.

To accurately measure the pitch of a sound you must sample many cycles. To analyze harmonics you want to sample few. The best result for real data will always be a compromise between range (bandwidth) and resolution. Both can be increased only by analyzing more points, which takes more time.

After experimenting with one sample at a time you will probably want to try continuous analysis. The input data pointer at hexadecimal address 0202 can be moved through an input buffer by the program that calls the transform. At roughly three seconds per transform, the data cannot suitably be analyzed in real time. A sample of a few seconds of data can be continuously analyzed and the changes slowly displayed. This is probably most easily accomplished by transferring the "sum of absolute value" data to a display buffer which is then scanned by an interrupt driven display program.

Bigger, Better, and Faster

Like most software, this program exists to be rewritten. No attempt was made to optimize execution speed. Preliminary experiments with an MMI-67658 hardware multiplier took slightly under one second. This relatively minor improvement was probably due to the time wasted in moving the data in and out of the multiplier. Perhaps it can be streamlined to the extent that a continuous display can be created. I plan to try a version for the 6502 microprocessor with hope of adding still more speed.

The algorithm is simple enough so that conversion should be easy. Enterprising 8080 and Z-80 enthusiasts shouldn't have too much trouble adapting the principles to their computers, either. Conversion to double precision or 512 to 1024 points should also be possible, although the present addressing scheme would have to be abandoned.

I hope this program will provide you with a tool that will be a lot of fun to play with. Please write and tell me what uses you find for it and any improvements you would like to suggest.

Continued on page 118

```

00286 035C 44          LSR A          DIVIDE IT BY 2
00287 035D 80 40      SUB A  #40     MAKE IT 2'S COMP.
00288 035F A7 00      STA A  0, X
00289 0361 08          INX           BUMP POINTER
00290 0362 5A          DEC B        NEXT POINT
00291 0363 26 F3      BNE  SCL6
00292 0365 33          PUL B
00293 0366 5A          DEC B        NEXT PAIR
00294 0367 26 EC      BNE  SCL5
00295 0369 39          RTS          RETURN
00296
00297
00298
*****
** 2'S COMP. MULTIPLY SUBR. **
*****
00299 036A 97 37      MPY  STA A  MPA+1  STORE MULTIPLIER
00300 036C 07 39      STA B  MPA+3  AND MULTIPLICAND
00301 036E 4F          CLR A
00302 036F 97 36      STA A  MPA     CLEAR MSB'S
00303 0371 97 38      STA A  MPA+2
00304 0373 97 34      STA A  MSBY    CLEAR PRODUCT
00305 0375 97 35      STA A  LSBY
00306 0377 50          TST B
00307 0378 2C 03      BGE  MPY1     NEGATIVE MULTIPLICAND ?
00308 037A 73 0038    COM  MPA+2    EXTEND NEG TO MSB
00309 037D 7D 0037    MPY1 TST  MPA+1
00310 0380 2C 03      BGE  MPY2     NEG MULTIPLIER ?
00311 0382 73 0036    COM  MPA     EXTEND NEG TO MSB
00312 0385 06 0F      MPY2 LDA B  #15   SET UP COUNTER
00313 0387 77 0036    MPY3 ASR  MPA     SHIFT X RIGHT
00314 038A 76 0037    ROR  MPA+1
00315 038D 24 0C      BCC  MPY4     BIT WAS ZERO
00316 038F 96 39      LDA A  MPA+3  ADD Y TO PRODUCT
00317 0391 9B 35      ADD A  LSBY
00318 0393 97 35      STA A  LSBY
00319 0395 96 38      LDA A  MPA+2  MSB'S
00320 0397 99 34      ADC A  MSBY
00321 0399 97 34      STA A  MSBY
00322 039B 78 0039    MPY4 ASL  MPA+3  SHIFT Y LEFT
00323 039E 79 0038    ROL  MPA+2
00324 03A1 5A          DEC B
00325 03A2 26 E3      BNE  MPY3
00326
**
00327
** SCALE IT UP **
00328
**
00329 03A4 96 34      LDA A  MSBY
00330 03A6 79 0035    ROL  LSBY
00331 03A9 49          ROL A
00332
**
00333
** RETURN WITH PRODUCT IN A
00334
**
00335 03AA 39          RTS
00336
*****
** END OF FFT PROGRAM **
*****
00337
00338
00339
END

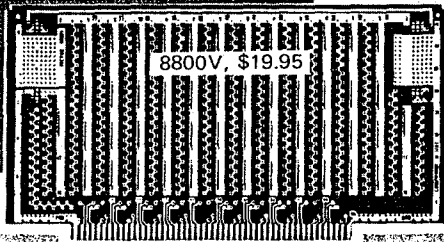
```

INPUT	0800	REALT	0500	IMAGT	0600	SINET	0400
RLPT1	0020	RLPT2	0022	IMPT1	0024	IMPT2	0026
SINPT	0028	CELNUM	002A	CELCT	002B	PAIRNM	002C
CELDIS	002D	DELTA	002E	SCLFCT	002F	COSA	0030
SINA	0031	TREAL	0032	TIMAG	0033	MSBY	0034
LSBY	0035	MPA	0036	INPD	0202	REAL	0204
IMAG	0206	SINE	0208	START	020A	CLEAR	020D
CLR1	0211	MOVE	0217	MOV1	0221	BITREV	0238
BRV1	023C	SWAP	0249	SWP1	0257	PASS1	025C
PA1	0264	FPASS	027A	NPASS	0286	NCELL	029B
NC1	02A2	NP1	031F	DONE	0330	SCALE	0333
SCL1	0337	SCL2	033A	SCL3	0345	SCL4	034D
SCL5	0355	SCL6	0358	MPY	036A	MPY1	037D
MPY2	0385	MPY3	0387	MPY4	039B		

TOTAL ERRORS 00000

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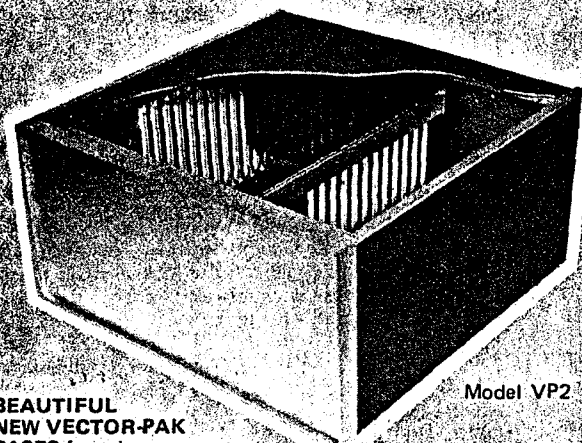
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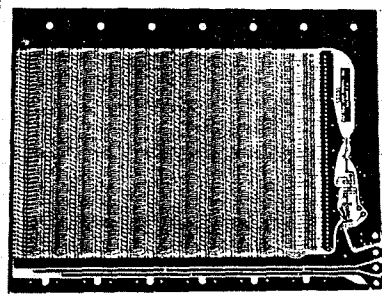
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BIBLIOGRAPHY

1. Brigham, E Oran, *The Fast Fourier Transform*, Prentice-Hall, Englewood Cliffs NJ, 1974.
2. Bryant, J, and Swasdee, M, "How to Multiply in a Wet Climate," *BYTE*, volume 3, number 4, April 1978, page 28.
3. Cooper, James W, *The Minicomputer in the Laboratory*, John Wiley and Sons Inc, New York, 1977.
4. Moorer, J, "On the Transcription of Musical Sound by Computer," *Computer Music Journal*, volume 1, number 4, November 1977, page 32.
5. Stearns, Samuel D, *Digital Signal Analysis*, Hayden Book Co Inc, Rochelle Park NJ, 1975.

Listing 2: The object code listing in hexadecimal format of the assembly language program given in listing 1. This listing can be used to manually enter the program or as a confirmation copy for the PAPERBYTE™ bar code representation given in figure 2. The format used for this listing is a 2 byte address field, followed by up to 16 bytes of data, with a 1 byte check digit at the end of each line. Note that the data in hexadecimal locations 0400 to 04FF constitute the sine and cosine lookup table which must be loaded with the transform subroutine.

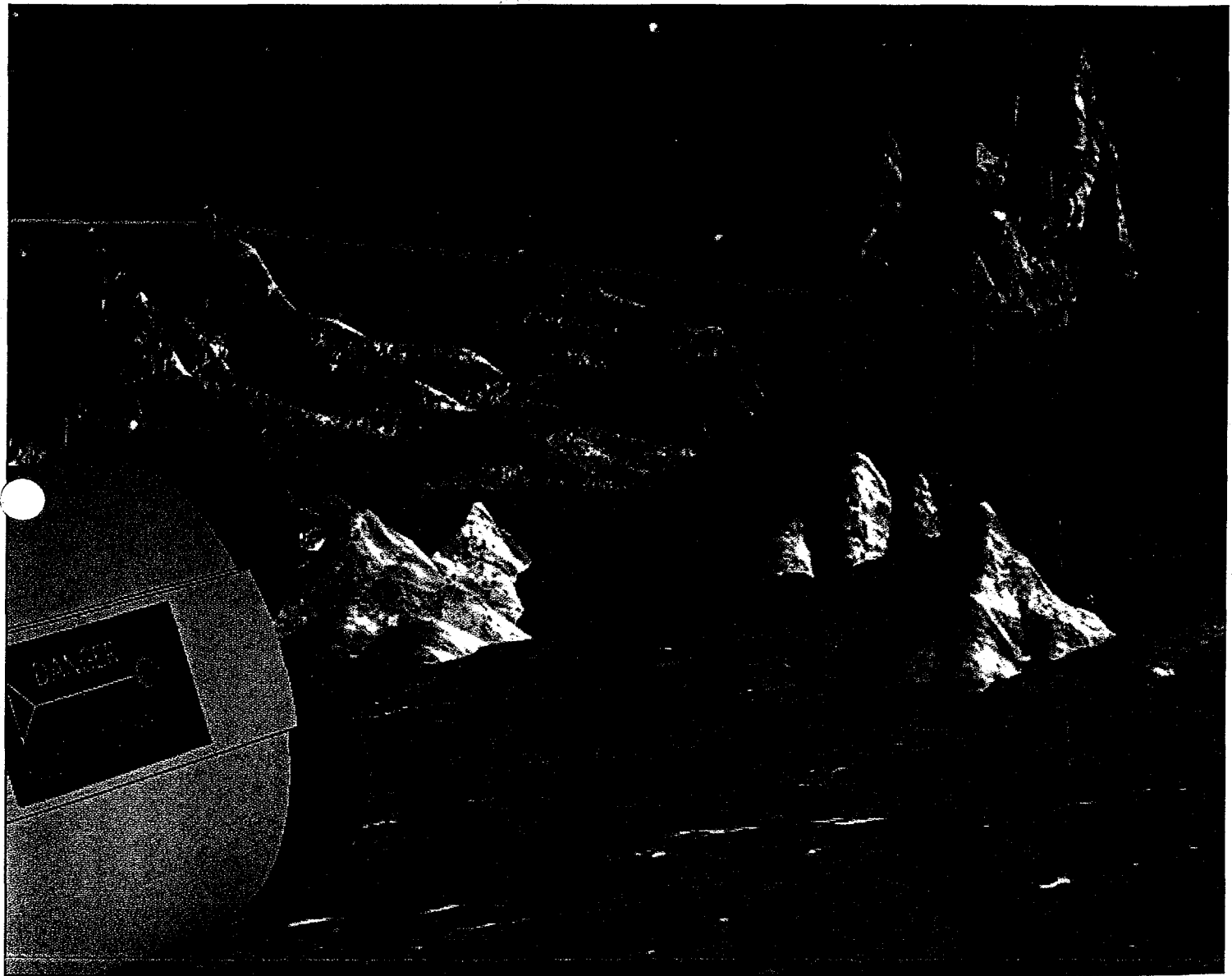
0200	20	08	08	00	05	00	06	00	04	00	7F	00	2F	FE	02	06	F3
0210	5F	6F	00	08	5A	26	FA	FE	02	02	DF	20	FE	02	04	DF	34
0220	22	DE	20	A6	00	08	DF	20	DE	22	A7	00	7C	00	23	26	39
0230	F0	FE	02	04	DF	20	DF	22	C6	08	96	21	46	79	00	23	5B
0240	5A	26	F9	96	23	91	21	25	0E	DE	20	A6	00	DE	22	E6	A1
0250	00	A7	00	DE	20	E7	00	7C	00	21	26	DC	BD	03	33	FE	1C
0260	02	04	DF	20	DE	20	A6	00	E6	01	36	1B	A7	00	32	10	CA
0270	A7	01	7C	00	21	7C	00	21	26	EA	86	40	97	2A	97	2E	3E
0280	86	02	97	2C	97	2D	BD	03	33	96	2A	97	2B	FE	02	04	88
0290	DF	20	DF	22	FE	02	06	DF	24	DF	26	FE	02	08	DF	28	1D
02A0	D6	2C	96	21	9B	2D	97	23	97	27	37	DE	28	A6	00	97	73
02B0	30	A6	40	97	31	DE	22	A6	00	36	D6	30	BD	03	6A	97	81
02C0	32	32	D6	31	BD	03	6A	97	33	DE	26	A6	00	36	D6	31	46
02D0	BD	03	6A	9B	32	97	32	32	D6	30	BD	03	6A	90	33	97	7C
02E0	33	DE	20	A6	00	16	9B	32	A7	00	DE	22	D0	32	E7	00	4A
02F0	DE	24	A6	00	16	9B	33	A7	00	DE	26	D0	33	E7	00	96	B7
0300	29	9B	2E	97	29	7C	00	21	7C	00	25	33	5A	26	93	96	CC
0310	21	9B	2D	97	21	97	25	7A	00	2B	27	03	7E	02	9B	74	BB
0320	00	2A	27	0C	78	00	2C	78	00	2D	74	00	2E	7E	02	86	4E
0330	39	00	00	FE	02	04	5F	37	C6	02	A6	00	08	81	C0	22	AC
0340	04	81	40	24	08	5A	26	F2	33	5A	26	EB	39	33	7C	00	E9
0350	2F	FE	02	04	5F	37	C6	02	A6	00	8B	80	44	80	40	A7	ED
0360	00	08	5A	26	F3	33	5A	26	EC	39	97	37	D7	39	4F	97	17
0370	36	97	38	97	34	97	35	5D	2C	03	73	00	38	7D	00	37	87
0380	2C	03	73	00	36	C6	0F	77	00	36	76	00	37	24	0C	96	CD
0390	39	9B	35	97	35	96	38	99	34	97	34	78	00	39	79	00	65
03A0	38	5A	26	E3	96	34	79	00	35	49	39						95
0400	7F	7F	7F	7F	7F	7F	7E	7E	7D	7D	7C	7B	7A	79	78	77	C9
0410	76	75	73	72	71	6F	6D	6C	6A	68	66	65	63	61	5E	5C	A4
0420	5A	58	56	53	51	4E	4C	49	47	44	41	3F	3C	39	36	33	78
0430	31	2E	2B	28	25	22	1F	1C	19	16	12	0F	0C	09	06	03	A2
0440	00	FD	FA	F7	F4	F1	EE	EA	E7	E4	E1	DE	DB	D8	D5	D2	8F
0450	CF	CD	CA	C7	C4	C1	BF	BC	B9	B7	B4	B2	AF	AD	AA	A8	B1
0460	A6	A4	A2	9F	9D	9B	9A	98	96	94	93	91	8F	8E	8D	8B	78
0470	8A	89	88	87	86	85	84	83	82	81	81	81	81	81	81	81	40
0480	81	81	81	81	81	81	82	82	83	83	84	85	86	87	88	89	37
0490	8A	8B	8D	8E	8F	91	93	94	96	98	9A	9B	9D	9F	A2	A4	5C
04A0	A6	A8	AA	AD	AF	B2	B4	B7	B9	BC	BF	C1	C4	C7	CA	CD	88
04B0	CF	D2	D5	D8	DB	DE	E1	E4	E7	EA	EE	F1	F4	F7	FA	FD	5E
04C0	00	03	06	09	0C	0F	12	16	19	1C	1F	22	25	28	2B	2E	71
04D0	31	33	36	39	3C	3F	41	44	47	49	4C	4E	51	53	56	58	4F
04E0	5A	5C	5E	61	63	65	66	68	6A	6C	6D	6F	71	72	73	75	88
04F0	76	77	78	79	7A	7B	7C	7D	7D	7E	7E	7F	7F	7F	7F	7F	C0

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